

$$y' = 4\sqrt{x}, \quad y(0) = 2$$

Integrate both sides:

$$\begin{aligned} y &= \int 4x^{\frac{1}{2}} = 4\left(\frac{2}{3}x^{\frac{3}{2}}\right) + C \\ &= \frac{8}{3}x^{\frac{3}{2}} + C \end{aligned}$$

Apply initial condition:

$$y(0) = \frac{8}{3}(0)^{\frac{3}{2}} + C = 2$$

$$\rightarrow C = 2$$

$$\text{So, } y = \frac{8}{3}x^{\frac{3}{2}} + 2$$